CANADA
DEPARTMENT OF FORESTRY AND RURAL DEVELOPMENT

# PROVISIONAL AERIAL STAND VOLUME TABLES FOR SELECTED FOREST TYPES IN CANADA 

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Résumé en français

FORESTRY BRANCH<br>DEPARTMENTAL PUBLICATION NO. 1175<br>1966


#### Abstract

Data from 1,933 field-measured sample plots in Quebec, Ontario, Northwest Territories and Alberta were used to construct aerial stand volume tables for 10 cover types by regression analysis. The tables, in which volume is predicted from stand height and canopy density, are sufficiently accurate for the determination of preliminary stand volume estimates.


## RÉSUMÉ

Ayant en main les données sur 1,933 places-échantillons qu'on avait établies entre 1951 et 1958 dans le Québec, l'Ontario, les Territoires du NordOuest et l'Alberta, l'auteur a construit des tables de volumes de peuplements en se servant de photographies aériennes récentes qu'il a interprétées par l'analyse des régressions. Dix types de peuplements furent traités et les tables, qui prédisent les volumes à partir de la hauteur du peuplement et la densité du couvert, sont considérées par l'auteur comme étant suffisamment précises pour servir à faire des estimations provisoires.

Published under the authority of The Honourable Maurice Sauvé, P.C., M.P., Minister of Forestry and Rural Development Ottawa, 1966

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## ACKNOWLEDGEMENTS

The author wishes to acknowledge the help of Dr. A. L. Wilson, Biometrics Research Services, Department of Forestry and Rural Development, in the regression analyses and in the establishment of criteria for the cover type stratification.

Also, efforts by other staff members in collecting and compiling the data over a long period of years, under the direction of Mr. H. E. Seely, are duly acknowledged.

# Provisional Aerial Stand Volume Tables for Selected Forest Types in Canada 

by<br>G. M. Bonnor ${ }^{1}$

## INTRODUCTION

The construction and use of aerial stand volume tables has become increasingly important in the last two decades, primarily due to improvements in aerial photographic techniques. The tables are based on the relationship between variables which can be measured or interpreted on aerial photographs and stand volume. They are used to estimate stand volumes from the photographs either directly or in conjunction with local field data to produce local volume tables.

The stand characteristics most commonly used to estimate stand volume from aerial photographs are: crown closure (canopy density), crown count, crown diameter and tree height (Spurr 1948). For construction of the tables, photo measurements of the independent variables are commonly used (Moessner et. al. 1951, Allison and Breadon 1958, Roger et. al. 1959); however, ground measurements (Nyyssonen 1955) or a combination of photo and ground measurements (Gingrich and Meyer 1955) have also been used.

The dependent variable, volume, is expressed in cubic feet or board feet, total volume or merchantable volume, depending on the required use of the tables. For construction of the tables, volume is usually determined by the application of field measurements to volume tables.

Stratification of the forest area into cover types by means of aerial photographs is usual and, if properly carried out, has the effect of reducing regression variance. Stratification by density, height, species, species groups, volume classes or site are common schemes. Moessner (1963) made a study of a number of photo and map stratification schemes; findings indicated that in volume estimating, photo volume classes offer the best means of stratification. Bickford (1953) in a similar study compared volume class stratification with stand size stratification and also found the former to be more efficient. Kendall and SaynWittgenstein (1961) in a test of the effectiveness of air photo stratification included some continuous variables more commonly found in regression equations. They found a stratification by cover type, height and canopy density to give the most precise volume estimates. Macpherson (1962) found a two-way stratification by cover type and volume class to give good volume predictions.

Of the parameters used to estimate stand volume from aerial photos, average stand height appears to be the best single variable (Hanks and Thomson 1964,

[^0]Nyyssonen 1955, Gingrich and Meyer 1955), although Morris (1957) assumed that the estimation of age and stand density would give more accurate volume estimates than height. Other parameters commonly used are canopy density and average crown diameter. Moessner et. al. (1951) found that, of the three parameters mentioned, canopy density showed the poorest over-all correlation with volume, but they included canopy density because of its value in stands of below medium density. Bickford (1953), however, dealing with the same variables, found canopy density to give the best volume estimates.

The precision of stand volume tables varies a great deal, depending on the homogeneity of the area sampled and the methods used in constructing the tables. The standard error of estimate, expressed in per cent of the mean volume, is often used to indicate the precision of the tables. Duffy and Meyer (1962) reported a low standard error of estimate of $\pm 17 \%$ for a table for lodge pole pine stands in Alberta; Hanks and Thomson (1964), on the other hand, reported standard errors of estimate in excess of $\pm 65 \%$ for Iowa hardwoods.

## THE STUDY

This report deals with the construction of stand volume tables for cover types in the Subalpine, Boreal and Great Lakes-St. Lawrence Regions of Canada (Rowe 1959). The basis for the tables is data from 1,933 sample plots, collected during the period 1951-1958. Further details of the sampling are given in Table 1.

TABLE 1. LOCATION AND COMPOSITION OF SAMPLE PLOTS

| Location | Latitude and Longitude |  | Forest Region | Major Species* | No. of Plots |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Matane, P.Q. | 49 | 67 | Boreal | bF,wB, bS, wS | 150 |
| Sault-au-Cochon, P.Q... | 49 | 69 | Boreal | bS,wP,rP | 39 |
| St. Maurice, P.Q. | 47 | 73 | Gt. Lakes-St. Lawrence | bS,jP | 111 |
| Lièvre, P.Q. | 47 | 75 | Gt. Lakes-St. Lawrence | $\begin{aligned} & \mathrm{yB}, \mathrm{bF}, \mathrm{bS}, \\ & \mathrm{jP}, \mathrm{hM}, \mathrm{Be} \end{aligned}$ | 465 |
| Algonquin, Ontario. | 46 | 78 | Gt. Lakes-St. Lawrence | wP, rP, jP | 382 |
| Dorset, Ontario........ | 45 | 79 | Gt. Lakes-St. Lawrence | hM, Be | 47 |
| Nipigon, Ontario. | 48 | 88 | Boreal | t.A.jP, bS | 199 |
| Peace River, Alberta... | 59 | 112 | Boreal | wS,bPo | 164 |
| Slave River, N.W.T... | 61 | 113 | Boreal | wS, bPo | 148 |
| Kananaskis, Alberta..... | 51 | 115 | Subalpine | $1 \mathrm{P}, \mathrm{wS}$ | 228 |
|  |  |  |  | Total | 1933 |

*for list of abbreviations, see Appendix 1.

The tables are based on the relationship between total cubic foot volume per acre (V), for trees four inches d.b.h. and up, and canopy density (C) and average stand height (H). Regression analyses were used to evaluate this relationship. All parameters were obtained from ground measurements.

## METHOD

The collection and compilation of basic data incorporate methods which may be challenged by statisticians and mensurationists. These sources of error will be dealt with separately. Also, because of the lengthy period over which the data were assembled and the large number of people working on the project, there was some variation in the method of collecting and compiling the data. However, the general procedure was as follows.

At the start of each field season, the cover types to be sampled were chosen. Following the selection of suitable sampling areas and stands, plot locations were subjectively established to provide a wide range of height, canopy density and site classes.

Sample plots were established in the selected locations. The square sample plots covered $1 / 4$ or $1 / 5$ acre. For each plot, the following information was recorded: site class, plant indicators, disturbances, soil moisture and texture, parent material, topography; forest section and region, drainage area, photo no., plot no., plot size, date; height class, canopy density class, cover type and age class. Further, a complete tally of trees was made by species, in one inch diameter classes, for trees four inches in diameter at breast height and over. Also, the height of five to ten trees was measured, and $30-60$ readings with a modification of the Moosehorn (Robinson 1947) were obtained for the determination of canopy density.

In the office, height-diameter curves were constructed by 10 foot mean height classes for each location and for each species. The plot volume as well as the average heights weighted by volume were then obtained by the application of the diameter tallies to local volume tables prepared from the height-diameter curves and form class volume tables (Anon. 1948). Also, the basal area for each species within each plot was calculated. Lastly, from the readings with the Moosehorn, canopy density (per cent crown cover) was calculated for each plot.

By application of the basal area figures for each plot to the sub-type classification used by the Department of Forestry and Rural Development, the subtype of each plot was determined. A total of 151 sub-types were represented by the 1933 plots. To provide a sufficient number of plots for the subsequent analyses, the plots were combined into 13 cover types, each containing at least 50 plots.

## ANALYSES AND INTERPRETATION

The variables included in the first regression analysis were:

$$
\begin{array}{ll}
\mathrm{Y}=\mathrm{V} \text { (volume per acre) } & \mathrm{X}_{5}=\frac{1}{\mathrm{C}} \\
\mathrm{X}_{1}=\mathrm{H} \text { (stand height, in feet) } & \mathrm{X}_{6}=\mathrm{C}^{2} \\
\mathrm{X}_{2}=\mathrm{C} \text { (canopy density, in per cent) } & \\
\mathrm{X}_{3}=\mathrm{HC} & \mathrm{X}_{7}=\frac{\mathrm{H}}{\mathrm{C}}
\end{array}
$$

A step-wise multiple regression analysis (Brown) ${ }^{2}$ was carried out for each cover type and for the combined data. Only the three variables showing the best correlation with stand volume were included in the evaluation of the regression analyses. Cover types and results of the analyses are shown in Table 2.

[^1]TABLE 2. RESULTS OF FIRST SERIES OF REGRESSION ANALYSES

| Cover Type |  | No. of Plots | Best 3 Variables |  | Standard Error |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | cu. ft. |  |  | $\%$ of volume |
| 100 | (All plots). |  | 1933 | H $\quad \frac{1}{\mathrm{C}}$ | $\mathrm{HC}^{2}$ | 995 | 33 |
| 101 | Intolerant hardwoods. | 87 | $\mathrm{H} \quad \mathrm{HC}^{2}$ | C | 766 | 20 |
| 102 | Tolerant hardwoods. | 338 | HC C | H | 541 | 21 |
| 103 | Intolerant hardwoods + softwoods. | 69 | $\mathrm{H} \quad \mathrm{C}^{2}$ |  | 672 | 20 |
| 104 | Tolerant hardwoods + softwoods.. | 51 | $\mathrm{HC} \mathrm{C}^{2}$ | H | 661 | 37 |
| 105 | Jack pine. | 249 | H $\quad \frac{\mathrm{H}}{\mathrm{C}}$ |  | 443 | 21 |
| 106 | Black spruce | 168 | $\mathrm{HC} \mathrm{C}^{2}$ | $\frac{\mathrm{H}}{\mathrm{C}}$ | 449 | 25 |
| 107 | White spruce. | 242 | H $\quad \mathrm{H}$ | C | 827 | 18 |
| 108 | Red and white pine. | 127 | $\mathrm{HC} \frac{\mathrm{H}}{\mathrm{C}}$ | $\mathrm{C}^{2}$ | 459 | 14 |
| 109 | Balsam fir. | 101 | $\mathrm{HC}^{2} \mathrm{C}$ | $\frac{\mathrm{H}}{\mathrm{C}}$ | 997 | 31 |
| 110 | Pine-Spruce. | 86 | $\frac{1}{\mathrm{C}} \quad \mathrm{H}$ |  | 893 | 27 |
| 111 | Spruce-Balsam. | 108 | $\mathrm{HC} \mathrm{HC}^{2}$ |  | 918 | 27 |
| 112 | Pine-Intolerant hardwoods. | 108 | HC $\frac{\mathrm{H}}{\mathrm{C}}$ |  | 611 | 18 |
| 113 | Lodgepole pine. | 199 | HC C | H | 519 | 19 |

The "Best 3 Variables" are listed in order of importance. The standard errors of estimate compare favourably with those obtained by other researchers (Hanks and Thomson 1964). However, the lack of any trend in the variables selected lead to the conclusion that there is little difference between the variables, and that any three variables that include height and canopy density will give a fit almost as good as the combinations in Table.2. For this reason, and to produce greater uniformity between regression equations, another series of regression analyses was calculated, using three selected variables. The variables selected were $\mathrm{H}, \mathrm{C}$ and HC , corresponding to the variables of the "Australian" equation (Spurr 1952). The standard errors of estimate obtained by the use of these variables were approximately the same as those shown in Table 2, and it was decided to use $\mathrm{H}, \mathrm{C}$ and HC in the volume equations.

The last series of tests investigated the possibility of combining some of the cover types without a significant loss of accuracy. Basic to this approach was the calculation of a regression equation common to all 1,933 plots. The error in total plot volume, had this equation been used, was then calculated for each cover

TABLE 3. RELATIVE ERROR IN VOLUME PREDICTION USING A COMMON REGRESSION

| Cover Type | Difference between field estimated volume and predicted volume (in \% of field estimated volume) |
| :---: | :---: |
| 101 Intolerant hardwoods | $+.4$ |
| 102 Tolerant hardwoods. | +29 |
| 103 Intolerant hardwoods + softwoods. | - 5.4 |
| 104 Tolerant hardwoods + softwoods. | +83 |
| 105 Jack pine. | +30 |
| 106 Black spruce. | + 2.6 |
| 107 White spruce. | -10 |
| 108 Red and white pine. | -8.1 |
| 109 Balsam fir. | -16 |
| 110 Pine-Spruce. | -14 |
| 111 Spruce-Balsam. | -19 |
| 112 Pine-Intolerant hardwoods. | $-8.5$ |
| 113 Lodgepole pine. | -25 |

type and expressed in per cent of total plot volume for that cover type. In Cover Type 105, for example, the sum of all plot volumes is $512,012 \mathrm{cu}$. ft . Using the common regression, the estimated total volume is $666,462 \mathrm{cu} . \mathrm{ft}$. The difference expressed in per cent of the sum of all plot volumes is $30 \%$. These errors, called relative errors, are shown in Table 3.

This approach was based on the assumption that cover types having similar relative errors in volume estimation could be combined and new equations calculated for the selected combinations. The error is relative only to the common equation and is removed when separate equations are calculated. The figures in Table 3 indicate that a number of combinations are possible (101, 106; 102, 105; $103,108,112 ; 109,110,111)$. However, allowing for the fact that sample data such as these do not completely reflect the relationships within populations, it was decided that such combinations should also be silviculturally meaningful. For example, Table 3 shows that cover types 102 (tolerant hardwoods) and 105 (jack pine) have similar relative errors. A combination of these two cover types, however, would not be silviculturally meaningful.

Taking the above considerations into account, it was decided to combine cover types 109, 110 and 111 into one cover type (114, mixed softwoods) and cover types 103 and 112 into another cover type (115, intolerant hardwoods + softwoods).

The regression coefficients and standard errors of estimate were then calculated (Table 4), and stand volume tables were constructed from the equations (Appendix II). In the tables, the range of the sample plot data is blocked by a heavy line.

TABLE 4. STAND VOLUME TABLE REGRESSION EQUATIONS

| Cover Type |  | Regression Equation | Standard error of estimate |  | No. of Plots |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | (cu.ft.) | $\begin{aligned} & \text { (\% of } \\ & \text { vol.) } \end{aligned}$ |  |
| 101 | Intolerant hardwoods. |  | $\begin{aligned} \mathrm{V}= & 824.274+8.11249 \mathrm{H} \\ & -52.9139 \mathrm{C}+1.18962 \mathrm{HC} \end{aligned}$ | 661 | 20 | 87 |
| 102 | Tolerant hardwoods. | $\begin{aligned} \mathrm{V}= & 2309.65-32.7908 \mathrm{H} \\ & -53.2246 \mathrm{C}+1.18467 \mathrm{HC} \end{aligned}$ | 535 | 21 | 338 |
| 104 |  | $\begin{aligned} \mathrm{V}= & -4844.11+89.2225 \mathrm{H} \\ & +85.2487 \mathrm{C}-1.11417 \mathrm{HC} \end{aligned}$ | 662 | 37 | 51 |
| 105 | Jack pine........................ | $\begin{aligned} \mathrm{V}= & -1467.76+35.8816 \mathrm{H} \\ & -16.8047 \mathrm{C}+.817067 \mathrm{HC} \end{aligned}$ | 454 | 21 | 249 |
| 106 | Black spruce. . . . . . . . . . . . . . . | $\begin{aligned} \mathrm{V}= & -877.070+29.5130 \mathrm{H} \\ & -13.6464 \mathrm{C}+.887888 \mathrm{HC} \end{aligned}$ | 454 | 25 | 168 |
| 107 | White spruce. . . . . . . . . . . . . . . | $\begin{aligned} \mathrm{V}= & -1103.17+53.9385 \mathrm{H} \\ & -7.26820 \mathrm{C}+.585915 \mathrm{HC} \end{aligned}$ | 832 | 18 | 242 |
| 108 | Red and white pine........... | $\begin{aligned} \mathrm{V}= & -7476.08+114.278 \mathrm{H} \\ & +85.2758 \mathrm{C}-.568079 \mathrm{HC} \end{aligned}$ | 462 | 14 | 127 |
| 113 | Lodgepole pine | $\begin{aligned} \mathrm{V}= & 1710.75-38.7005 \mathrm{H} \\ & -48.7927 \mathrm{C}+2.29914 \mathrm{HC} \end{aligned}$ | 668 | 19 | 199 |
| 114 | Mixed softwoods | $\mathrm{V}=-5282.70+106.799 \mathrm{H}$ | 995 | 30 | 295 |
| 115 | ```Intolerant hardwoods + soft- woods``` | $\begin{aligned} \mathrm{V}= & -5983.88+112.174 \mathrm{H} \\ & +62.2359 \mathrm{C}-.495664 \mathrm{HC} \end{aligned}$ | 656 | 20 | 177 |

It should be noted that the equation for cover type 107, white spruce, which contains plot data from Quebec, Northwest Territories and Alberta, has a relatively low standard error, indicating that the relationship between volume, canopy density and height is not significantly affected by regional differences.

The stereograms in Table 5 illustrate three of the sub-types and cover types for which the tables were constructed. The data accompanying each stereogram were obtained from ground measurements. The information in the table therefore provides the user with some indication of the appearance on aerial photographs of ground-measured stand characteristics.

## SOURCES OF ERROR

The choice of stand characteristics, the collection of sample plot data and the compilation methods have all contributed to weaknesses in the regression equations and volume tables. These sources of error should be explained, in order that better use be made of the tables.

The plot selection method described previously is extremely subjective. Within each cover type, the plots were selected, not located at random, to provide a wide range of height, canopy density and site classes. The samples therefore could yield information about the population which is biased. However, from a practical point of view the method affords a better-than-average coverage of the desired classes.


Corex type blek spruce
Wetmaked wolume : why critace


Covex trow maxd sotwools (1)






Cover typer therant mardwoots (102)



[^2]Another potential source of error is the use of average height weighted by volume (MacAndrews 1955). In theory the use of this variable in aerial stand volume tables is improper, since knowledge of stand volume prior to the determination of this average height is necessary. In the application of most stand volume tables, however, average stand heights are estimated and an experienced photo interpreter could produce estimates of average height weighted by volume as accurate as those of other average heights. Average height weighted by volume is generally close to the average height of dominants and codominants for a given stand (MacAndrews 1955).

Concerning Moosehorn readings, current research ${ }^{3}$ indicates that 100-300 Moosehorn readings are necessary to obtain canopy density estimates within 5 per cent canopy density of the actual canopy density, with a probability level of 95. The much smaller number of readings obtained in the sample plots therefore has produced inaccurate canopy density values. However, the large number of sample plots may have reduced the effect of this inaccuracy on the regression analyses. The research project referred to above also indicates that the Moosehorn does not yield biased canopy density estimates.

The use of ground measurements eliminates one source of bias common to methods in which photo measurements of stand characteristics are used, namely the personal bias of the photo interpreter. For the same reason, another source of bias is introduced: in the application of the tables, canopy density is measured on aerial photos, and we have no assurance that this photo-measured characteristic is the same as the ground-measured canopy density.

## CONCLUSIONS

The results of the regression analyses support the findings by some other researchers, namely that both height and canopy density are useful variables in the estimation of stand volume. Some cover types show evidence of decreasing volume with height and/or canopy density at the outer limits of the tables (cover types $101,102,104$ ). This tendency results largely from the fact that there were few plots in these classes and that the plots were given little weight in the regression analyses; it may also be in part attributed to over-maturity associated with hardwood stands. The successful combination of several species and species groups into one cover type indicate that, for the rough estimation of stand volume, only a few cover types are necessary, and makes easier the job of the photo interpreter, who does not have to distinguish between as many species.

While the stand volume tables presented in this study suffer from certain shortcomings, it is believed that they will find a useful application in the field of preliminary volume estimates. The tables will be useful in the initial, rough estimation of individual stand volumes and in the stratification of stands by volume classes (Moessner 1963). Also, they will provide a framework for the construction of local volume tables.

[^3]
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## APPENDIX I <br> SPECIES NAMES AND ABBREVIATIONS

| Common Name | Abbreviation | Latin Name |
| :---: | :---: | :---: |
| Eastern white pine. | wP | Pinus strobus L. |
| Red pine. | rP | Pinus resinosa Ait. |
| Jack pine. | jP | Pinus banksiana Lamb. |
| Lodgepole pine. | 1 P | Pinus contorta Dougl. var. latifolia Engelm. |
| Black spruce | bS | Picea mariana (Mill.) BSP |
| White spruce | wS | Picea glauca (Moench) Voss. |
| Balsam fir | bF | Abies balsamea (L.) Mill. |
| Tamarack | tL | Larix laricina (Du Roi) K. Koch |
| Eastern white cedar | eC | Thuja occidentalis L. |
| Eastern hemlock | eH | Tsuga canadensis (L.) Carr. |
| Trembling aspen | tA | Populus tremuloides Michx. |
| Largetooth aspen | 1 A | Populus grandidentata Michx. |
| Balsam poplar | bPo | Populus balsamifera L. |
| White birch. | wB | Betula papyrifera Marsh. |
| Yellow birch | yB | Betula alleghaniensis Britt. |
| Sugar maple. | sM | Acer saccharum Marsh. |
| Red maple. | rM | Acer rubrum L. |
| Ash. | As | Fraxinus americana L. |
| Basswood | Ba | Tilia americana L. |
| Beech | Be | Fagus grandifolia Ehrh. |
| Cherry | Ch | Prunus serotina Ehrh. |
| Elm. | E | Ulmus americana L. |
| Ironwood. | I | Ostrya virginiana (Mill.) K. Koch |
| Oak | O | Quercus alba L. and Quercus rubra L. |

## APPENDIX II

## AERIAL STAND VOLUME TABLES

Cover Type 101
Intolerant Hardwoods

| Canopy <br> Density in Per Cent | Stand Height, in feet |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 40 | 50 | 60 | 70 | 80 | 90 | 100 |
|  | Volume per acre of trees $4^{\prime \prime}$ d.b.h. and over in total cubic feet |  |  |  |  |  |  |
| 40 | 936 | 1492 | 2050 | 2606 | 3164 | 3720 | 4277 |
| 50 | 882 | 1558 | 2234 | 2910 | 3586 | 4262 | 4938 |
| 60 | 829 | 1624 | 2419 | 3214 | 4009 | 4804 | 5598 |
| 70 | 776 | 1690 | 2603 | 3517 | 4431 | 5345 | 6259 |
| 80 | 722 | 1755 | 2788 | 3821 | 4854 | 5886 | 6919 |
| 90 | 669 | 1821 | 2973 | 4124 | 5276 | 6428 | 7580 |

Basis: 87 plots
Location: Lièvre, P.Q. ( 2 plots)
Algonquin, Ont. ( 1 plot)
Nipigon, Ont. (14 plots)
Peace River, Alta. (41 " )
Slave River, N.W.T. (29 " )
Regression equation: $\mathrm{V}=824.274+8.11249 \mathrm{H}-52.9139 \mathrm{C}+1.18962 \mathrm{HC}$
Standard error of estimate $: \pm 20 \%$
Average species composition*:
bPo $85 \%$
tA $12 \%$
other 3\%

[^4]Cover Type 102
Tolerant Hardwoods

| $\begin{gathered} \text { Canopy } \\ \text { Density } \\ \text { in Per Cent } \end{gathered}$ | Stand Height, in feet |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 40 | 50 | 60 | 70 | 80 |
|  | Volume per acre of trees $4^{\prime \prime}$ d.b.h. and over in total cubic feet |  |  |  |  |
| 20 | 881 | 790 | 699 | 608 | 517 |
| 30 | 823 | 850 | 878 | 905 | 933 |
| 40 | 764 | 910 | 1056 | 1202 | 1348 |
| 50 | 706 | 970 | 1235 | 1499 | 1764 |
| 60 | 648 | 1031 | 1414 | 1796 | 2179 |
| 70 | 589 | 1091 | 1592 | 2093 | 2595 |
| 80 | 531 | 1151 | 1771 | 2390 | 3010 |
| 90 | 473 | 1211 | 1949 | 2688 | 3426 |
| 100 | 414 | 1271 | 2128 | 2984 | 3841 |

Basis: 338 plots
Location: Lièvre, P.Q. (285 plots)
Algonquin, Ont. ( 8 ")
Dorset, Ont. ( 45 " )
Regression equation $: \mathrm{V}=2309.65-32.7908 \mathrm{H}-53.2246 \mathrm{C}+1.18467 \mathrm{HC}$
Standard error of estimate: $\pm 21 \%$
Average species composition:
sM $58 \%$
Be $19 \%$
yB $17 \%$
other $6 \%$

## Cover Type 104

## Tolerant Hardwoods plus Softwoods

|  | Stand Height, in feet <br> Canopy <br> iensity <br> in Per Cent |  |  |  | 40 |
| :---: | :---: | :---: | :---: | :---: | :---: |

Basis: 51 plots
Location: Lièvre, P.Q. (46 plots)
Algonquin, Ont. ( 5 " )
Regression equation $: \mathrm{V}=-4844.11+89.2225 \mathrm{H}+85.2487 \mathrm{C}-1.11417 \mathrm{HC}$
Standard error of estimate: $\pm 37 \%$
Average species composition:

$$
\begin{array}{cc}
\text { yB } & 56 \% \\
\text { bF } & 17 \% \\
\mathrm{sM} & 10 \%
\end{array}
$$

Other softwoods $12 \%$
Other hardwoods 5\%

## Cover Type 105

Jack Pine

| $\begin{gathered} \text { Canopy } \\ \text { Density } \\ \text { in Per Cent } \end{gathered}$ | Stand Height, in feet |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 30 | 40 | 50 | 60 | 70 | 80 |
|  | Volume per acre of trees $4^{\prime \prime}$ d.b.h. and over in tetal cubic feet |  |  |  |  |  |
| 20 | - | 285 | 807 | 1330 | 1852 | 2374 |
| 30 | - | 444 | 1048 | 1652 | 2256 | 2860 |
| 40 | - | 603 | 1288 | 1974 | 2660 | 3345 |
| 50 | - | 761 | 1529 | 2296 | 3063 | 3831 |
| 60 | 71 | 920 | 1769 | 2618 | 3467 | 4316 |
| 70 | 148 | 1079 | 2010 | 2940 | 3871 | 4802 |
| 80 | 225 | 1238 | 2250 | 3263 | 4275 | 5288 |

Basis: 249 plots
Location: St. Maurice, P.Q. ( 62 plots)
Lièvre, P.Q. ( 44 " )
Algonquin, Ont. (105 " )
Nipigon, Ont. ( 38 " )
Regression equation: $\mathrm{V}=-1467.76+35.8816 \mathrm{H}-16.8047 \mathrm{C}+.817067 \mathrm{HC}$
Standard error of estimate: $\pm 21 \%$
Average species composition:

$$
\begin{array}{rr}
\text { jP } & 93 \% \\
\text { other } & 7 \%
\end{array}
$$

Cover Type 106

## Black Spruce

| Canopy <br> Density <br> in Per Cent | 30 | 40 | Stand Height, in feet |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |

Basis: 168 plots
Location: Matane, P.Q. ( 1 plot)
Sault-au-Cochon, P.Q. (30 plots)

| St. Maurice, P.Q. | $\left(\begin{array}{ll}7 & "\end{array}\right)$ |  |
| :--- | :--- | :--- |
| Lièvre, P.Q. | $(31$ | $")$ |
| Algonquin, Ont. | $(6$ | $")$ |
| Nipigon, Ont. | $(93$ | $")$ |

Regression equation: $\mathrm{V}=-877.070+29.5130 \mathrm{H}-13.6464 \mathrm{C}+.887888 \mathrm{HC}$
Standard error of estimate $: \pm 25 \%$
Average species composition:
bS $94 \%$
other $6 \%$

Cover Type 107
White Spruce

| Canopy <br> Density in Per Cent | Stand Height, in feet |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 50 | 60 | 70 | 80 | 90 | 100 | 110 | 120 |
|  | Volume per acre of trees $4^{\prime \prime}$ d.b.h. and over in total cubic feet |  |  |  |  |  |  |  |
| 20 | 2034 | 2691 | 3347 | 4004 | 4660 | 5317 | 5974 | 6630 |
| 30 | 2254 | 2970 | 3685 | 4400 | 5115 | 5830 | 6546 | 7260 |
| 40 | 2475 | 3249 | 4022 | 4796 | 5570 | 6344 | 7117 | 7891 |
| 50 | 2695 | 3527 | 4360 | 5192 | 6024 | 6857 | 7689 | 8522 |
| 60 | 2915 | 3806 | 4697 | 5588 | 6479 | 7370 | 8261 | 9152 |

Basis: 242 plots
Location: Peace River, Alta. (123 plots)
Slave River, N.W.T. (119 " )
Regression equation: $\mathrm{V}=-1103.17+53.9385 \mathrm{H}-7.2682 \mathrm{OC}+.585915 \mathrm{HC}$
Standard error of estimate: $\pm 18 \%$
Average species composition:
wS $98 \%$
other $2 \%$

Cover Type 108

## Red and White Pine

| Canopy <br> Density in Per Cent | Stand Height, in feet |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | 50 | 60 | 70 | 80 |
|  | Volume per acre of trees $4^{\prime \prime}$ d.b.h. and over in total cubic feet |  |  |  |
| 60 | 1650 | 2452 | 3254 | 4056 |
| 70 | 2219 | 2964 | 3709 | 4056 |
| 80 | 2788 | 3476 | 4164 | 4852 |
| 90 | 3356 | 3988 | 4619 | 5251 |

Basis: 127 plots
Location: Algonquin, Ont. (127 plots)
Regression equation: $\mathrm{V}=-7476.08+114.278 \mathrm{H}+85.2758 \mathrm{C}-.568079 \mathrm{HC}$
Standard error of estimate: $\pm 14 \%$
Average species composition:
rP $54 \%$
wP $35 \%$
hardwoods $7 \%$
other softwoods 4\%

## Cover Type 113

Lodgepole Pine

| $\begin{gathered} \text { Canopy } \\ \text { Density } \\ \text { in Per Cent } \end{gathered}$ | Stand Height, in feet |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 30 | 40 | 50 | 60 | 70 |
|  | Volume per acre of trees $4^{\prime \prime}$ d.b.h. and over in total cubic feet |  |  |  |  |
| 20 | 953 | 1026 | 1099 | 1172 | 1245 |
| 30 | 1155 | 1458 | 1761 | 2063 | 2366 |
| 40 | 1357 | 1890 | 2422 | 2955 | 3488 |
| 50 | 1559 | 2321 | 3084 | 3846 | 4609 |
| 60 | 1761 | 2753 | 3746 | 4738 | 5730 |
| 70 | 1962 | 3185 | 4407 | 5630 | 6852 |

Basis: 199 plots
Location: Kananaskis, Alta. (199 plots)
Regression equation: $\mathrm{V}=1710.75-38.7005 \mathrm{H}-48.7927 \mathrm{C}+2.29914 \mathrm{HC}$
Standard error of estimate $: \pm 19 \%$
Average species composition:
IP $97 \%$
other $3 \%$

## Cover Type 114

## Mixed Softwoods

| Canopy Density in Per Cent | Stand Height, in feet |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 40 | 50 | 60 | 70 | 80 |
|  | Volume per acre of trees $4^{\prime \prime}$ d.b.h. and over in total cubic feet |  |  |  |  |
| 10 | 3 | 518 | 1525 | 2532 | 3538 |
| 20 | 35 | 980 | 1925 | 2870 | 3815 |
| 30 | 557 | 1441 | 2325 | 3208 | 4092 |
| 40 | 1080 | 1902 | 2724 | 3547 | 4369 |
| 50 | 1603 | 2364 | 3124 | 3885 | 4646 |
| 60 | 2126 | 2825 | 3524 | 4223 | 4922 |
| 70 | 2648 | 3286 | 3924 | 4562 | 5199 |
| 80 | 3171 | 3747 | 4324 | 4900 | 5476 |
| 90 | 3694 | 4209 | 4724 | 5238 | 5753 |
| 100 | 4216 | 4670 | 5123 | 5577 | 6030 |

Basis: 295 plots
Location: Matane, P.Q. (149 plots)
Sault-au-Cochon, P.Q. ( 9 " ) St. Maurice, P.Q. ( 42 " )
Lièvre, P.Q. ( 48 " )
Algonquin, Ont. ( 5 " )
Nipigon, Ont. ( 17 " )

Kananaskis, Alta. ( 25 " )
Regression equation: $\mathrm{V}=-5282.70+106.799 \mathrm{H}+76.8578 \mathrm{C}-.614612 \mathrm{HC}$
Standard error of estimate $: \pm 30 \%$
Average species composition:

| bF | $52 \%$ | jP | $8 \%$ |
| ---: | ---: | ---: | ---: |
| bS | $14 \%$ | 1 P | $7 \%$ |
| wS | $11 \%$ | other | $8 \%$ |

## Cover Type 115

## Intolerant Hardwoods plus Softwoods

|  | Stand Height, in feet |  |  |
| :---: | :---: | :---: | :---: |
| Canopy <br> Density <br> in Per Cent | 50 | 60 | 70 |

Basis: 177 plots
Location: Lièvre, P.Q. ( 9 plots)
Algonquin, Ont. (125 " )
Dorset, Ont. (rr)
Nipigon, Ont.
Kananaskis, Alta. ( $\left.\begin{array}{rll}37 & \text { " } \\ 4 & "\end{array}\right)$
Regression equation: $\mathrm{V}=-5983.88+112.174 \mathrm{H}+62.2359 \mathrm{C}-.495664 \mathrm{HC}$
Standard error of estimate : $\pm 20 \%$
Average species composition:
tA $28 \%$
wP $23 \%$
rP $17 \%$
wB $10 \%$
bF $5 \%$
other softwoods $12 \%$
other hardwoods 5\%


[^0]:    ${ }^{1}$ Research Officer, Forest Management Research and Services Institute, Department of Forestry and Rural Development, Ottawa.

[^1]:    ${ }^{2}$ Brown, D. M. 1961. Least Squares Linear Regression Analysis for 1 Dependent and 24 Independent Variables. Department of Forestry and Rural Development of Canada. Statistical Research Service, Forest Entomology and Pathology Branch. File No. 06-01-001.

[^2]:    Cumpy density: 59\%
    Stakd haveran Th
    

[^3]:    ${ }^{3}$ Department of Forestry and Rural Development, Forest Management Research and Services Institute, Project 33-11-S2.

[^4]:    *by basal area, expressed in per cent of total basal area.

